

# Color-Induced Displacement double stars in SDSS<sup>★</sup>

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**Abstract.** We report the first successful application of the astrometric color-induced displacement technique (CID, the displacement of the photocenter between different bandpasses due to a varying contribution of differently colored components to the total light), originally proposed by Christy et al. (1983) for discovering unresolved binary stars. Using the Sloan Digital Sky Survey (SDSS) Data Release 2 with  $\sim 4.1 \times 10^6$  stars brighter than  $21^m$  in the  $u$  and  $g$  bands, we select 346 candidate binary stars with CID greater than 0.5 arcsec. The SDSS colors of the majority of these candidates are consistent with binary systems including a white dwarf and any main sequence star with spectral type later than  $\sim K7$ . The astrometric CID method discussed here is complementary to the photometric selection of binary stars in SDSS discussed by Smolčić et al. (2004), but there is considerable overlap (15%) between the two samples of selected candidates. This overlap testifies both to the physical soundness of both methods, as well as to the astrometric and photometric quality of SDSS data.

**Key words.** astrometry – stars: binaries: general

## 1. Introduction

It is believed that 50% of all stars belong to multiple systems (Heintz 1969). Nevertheless, being aware that a specific star is a binary is always useful because either one throws it out of the sample or updates the model to describe it and begins some follow-up observations! Whether one deals with stellar evolution or galactic dynamics, binaries always receive some special considerations. So, it is important to be able to detect the binary nature of a star at an early stage of an investigation by any possible means.

Besides spectroscopy, photometry, and interferometry, astrometry coupled to photometry has lately emerged as a way of revealing the binary nature of a source (Christy et al. 1983; Sorokin & Tokovinin 1985; Wielen 1996; Bailey 1998). That method relies upon either a change in the position of the source as its brightness varies (Variability-Induced Movers, VIM) or a photometric-band dependence of the position (Color-Induced Displacement, CID). We here adopt Wielen’s terminology rather than Chromatic Position Difference or Spectro-Astrometry. Whereas VIM requires several observations along the brightness variation cycle and only works when at least one

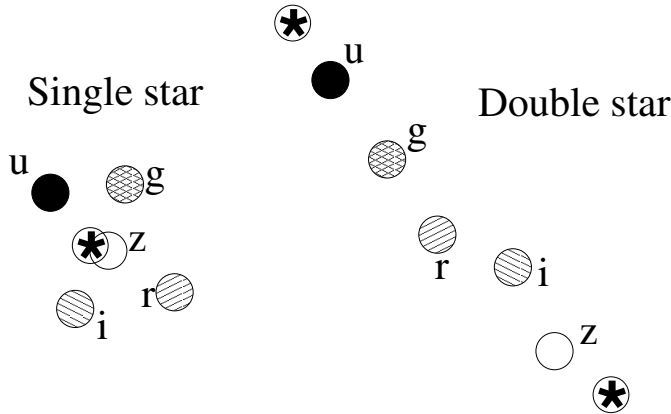
component is variable, it only takes one image in each band to identify a CID and can be done for non-variable stars. Despite the number of multi-band photometric surveys, none so far has carried sufficiently accurate astrometry in at least two distinct bands. This lack of observations has been recently alleviated by the Sloan Digital Sky Survey.

The Sloan Digital Sky Survey (SDSS; York et al. 2000; Abazajian et al. 2004, and references therein) is revolutionizing stellar astronomy by providing homogeneous and deep ( $r < 22.5$ ) photometry in five passbands ( $u$ ,  $g$ ,  $r$ ,  $i$ , and  $z$ ; Fukugita et al. 1996; Gunn et al. 1998; Hogg et al. 2001; Smith et al. 2002) accurate to 0.02 mag (Ivezić et al. 2003) down to  $g \sim 20.5$ . Ultimately, up to 10 000 deg<sup>2</sup> of sky in the Northern Galactic Cap will be surveyed. The survey sky coverage will result in photometric measurements for over 100 million stars and a similar number of galaxies. Astrometric positions are accurate to better than 0.1 arcsec per coordinate (rms) for point sources with  $r < 20.5^m$  (Pier et al. 2003), and the morphological information from the images allows robust star-galaxy separation to  $r \sim 21.5^m$  (Lupton et al. 2003).

Using the SDSS data, we report on the first successful identification of Color-Induced Displacement binaries. The underlying ideas of that method are given in Sect. 2. Section 3 describes the simulation that allowed us to optimize the screening of the data described in Sect. 4. In Sect. 5, we present our results and compare them with those of Smolčić et al. (2004),

<sup>★</sup> Table 1 is only available in electronic form at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsweb.u-strasbg.fr/cgi-bin/qcat?J/A+A/423/755>

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**Fig. 1.** Schematic position of the photocenter in the different SDSS bands. For double stars, the positions are aligned with the two stars and their order follows the central wavelength of the filter. Measurement error prevents the positions from being perfectly superposed/aligned for a single/double star. The true position of the star(s) is represented as a five-branch “star”.

who have recently used color selection to identify a stellar locus made of white dwarf+M dwarf binaries.

## 2. Color induced displacement

For any double star and any photometric filter, the position of the photocenter lies between the two components. If the two components have different colors, the position of the photocenter will change with the adopted filter as it depends on the ratio of the flux of the two components. The color-induced displacement is the change of the position of an unresolved binary depending on the adopted filter (Fig. 1).

Though Wielen (1996) suggested that variability induced motion and color induced motion could reveal the binary nature of an unresolved star, only the first approach has been applied to date, in the framework of Hipparcos (Wielen 1996; ESA 1997; Pourbaix et al. 2003). However, during the preparation of the Tycho-2 catalogue (Høg et al. 2000), Tycho and 2MASS (Skrutskie 1997) positions were compared. Source duplicity came up as a satisfactory explanation for most of the discrepant positions (S. Urban & V. Makarov, priv. comm.).

In the case of SDSS, the position and magnitude are measured in five bands (Pier et al. 2003). Even after the chromaticity effects have been accounted for, the five positions of a single star do not superpose exactly owing to measurement error (left panel of Fig. 1). For double stars,  $u$  and  $z$  photometric bands will yield the two positions which are the most separated because of the largest central wavelength difference between these two filters (right panel).

The position of the photocenter follows the peak of the efficiency of the filter. Therefore, the photocenters are not only aligned but also ordered by the filter effective wavelengths. The  $r$  band therefore plays a central role even if the  $r$  photocenter does not necessarily lie right at the middle of the  $u$  and  $z$  photocenters. Instead of requiring that the  $u$ -,  $r$ -, and  $z$ -photocenters are aligned and well ordered,

one can require that the angle measured from the  $r$ -position between  $u$  and  $z$  is  $180^\circ$ .

From now on, we will refer to the  $(u, z)$  angle as the angle measured from the  $r$ -position between  $u$  and  $z$ . The distance between  $u$  and  $z$  (noted  $\|(u, z)\|$ ) will refer to the angular separation between the position of the photocenter measured in the  $u$  and  $z$  band, respectively.

We do not use the  $g$ - and  $i$ -positions because the scatter on the  $g$ - and  $i$ -photocenter is not significantly smaller than on the  $u$  and  $z$  positions, thus leading to a lower signal-to-noise ratio (S/N) as far as  $\|(g, i)\|$  is concerned.

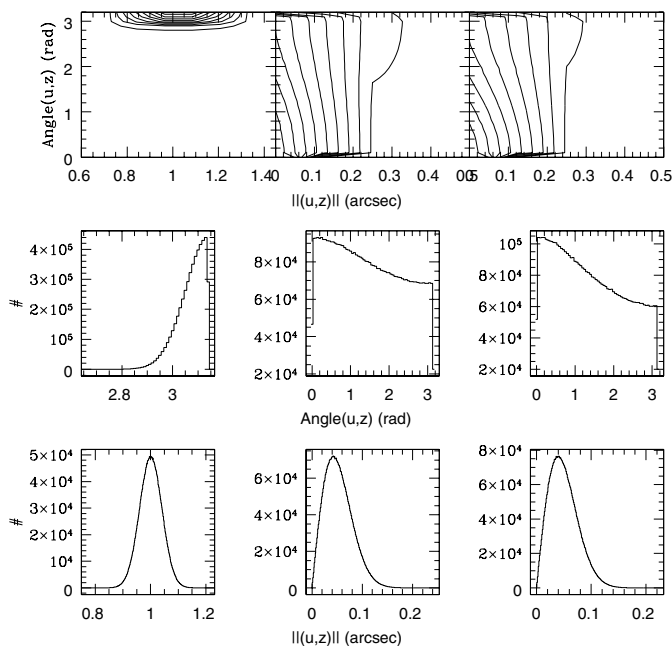
## 3. Simulations

In order to develop expectations for the relevant parameter space, we first carry out some simulations with noise properties consistent with the actual data, to estimate a lower bound of the separation we can expect to notice. According to Pier et al. (2003), the standard deviation on the relative position, i.e. band-to-band, for objects brighter than  $r \sim 20$  mag is 31 mas in  $u$  and 27 mas in  $z$  but the authors did not quote any correlation between the residuals in those two bands.

A parent population of  $\sim 2.4 \times 10^6$  stars with  $u < 21$  and  $g < 21$  and good photometry (see next section for details) was therefore used to update the precision of the residuals and to derive the correlation between them. The residuals in right ascension in  $u$  and  $z$  have a standard deviation of respectively 36 and 20 mas, with a correlation of 0.16. In declination, these precisions are 39 and 22 mas for  $u$  and  $z$  with a correlation of 0.18.

For the simulation, the position in the  $r$  band is assumed to lie in the middle of the segment joining the true photocenters in  $u$  and  $z$ . The distributions of the angle and separation between the  $u$ - and  $z$ -positions are derived from 5 million model positions generated for both photocenters using the above standard deviations and correlations. Such distributions for separations of  $1''$ , 20 mas and 0 mas are plotted in Fig. 2. The spread in the angle increases as the true separation goes to zero. Using a 99.9% confidence level Kolmogorov-Smirnov test, we reject the hypothesis that the marginal distributions of  $(u, z)$  for single stars and binaries with separations below 10 mas are different. It is worth noting that in the latter case, the correlation between the  $u$ - and  $z$ -positions prevents the angles from being uniformly distributed over  $0-\pi$ .

Though the percentage of binaries is usually thought to be quite high (ranging from 85% among OB stars, Heintz 1969; down to 30% for M stars, Marchal et al. 2003), very few binaries actually induce a noticeable shift of the photocenter. While the color induced displacement is larger the more different the colors, too large a magnitude difference causes the fainter component to be undetectable. Thus only a small fraction of true binaries will show detectable CID. Coupled to the spread of the angle due to measurement error, this means that one should not expect a large deviation of the distribution with respect to that of a pure single star population, especially if one looks at the whole SDSS sample.



**Fig. 2.** Model distribution of the angles and separations between the photocenters in  $u$  and  $z$  assuming a true separation of  $1''$  (left column),  $20$  mas (central column) and  $0$  mas (right column). Each line in the contour (top panels) represents a linear 10% increment. The bottom panels are the marginal distribution of the top panel row.

#### 4. Data

In this study, we use the public SDSS data release 2 (DR2) which contains 36 million stars. Because errors are larger towards fainter magnitudes, we selected stars to be bright enough to have good astrometry ( $u, g < 21$ ), thus reducing the number of stars to  $\sim 4.1 \times 10^6$ . We further impose

1. the condition that the displacement between the  $u$ - and  $z$ -positions is larger than  $0.2''$ . This criterion is expressed as:

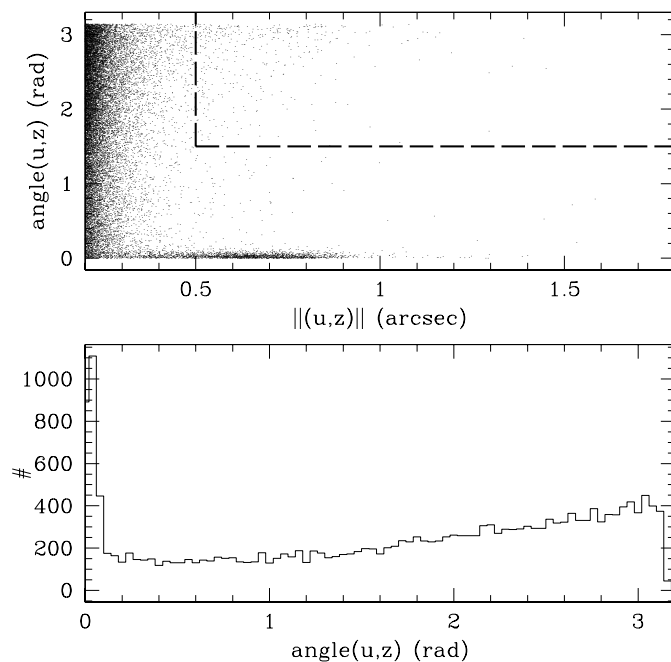
$$\sqrt{(\Delta\alpha_u - \Delta\alpha_z)^2 \cos^2 \delta + (\Delta\delta_u - \Delta\delta_z)^2} \geq 0.2$$

where the four offset quantities and the declination are readily available in the SDSS database;

2. the precision on the magnitudes is better than  $0.1$  mag in  $u$  and  $r$  and better than  $0.05$  mag for  $g, i$  and  $z$ .

Because astrometry and photometry are strongly tied together, bad photometry is likely to show up as poor astrometry anyway so these constraints on the photometric precision are actually safeguards for the astrometry as well. These two criteria yield a sample of only 24 908 entries,  $\sim 0.6\%$  of the previous sample. Further screening based on some quality control flags is also performed. The actual transact-SQL code submitted to DR2 is listed in Appendix A.

The angles versus the separations between the  $u$ - and  $z$ -photocenters the distribution of the latter are plotted in Fig. 3. With respect to the simulations from Sect. 3, there is a strong excess of points with a large displacement but with a  $0$  angle. This very striking feature is due to asteroids. Both

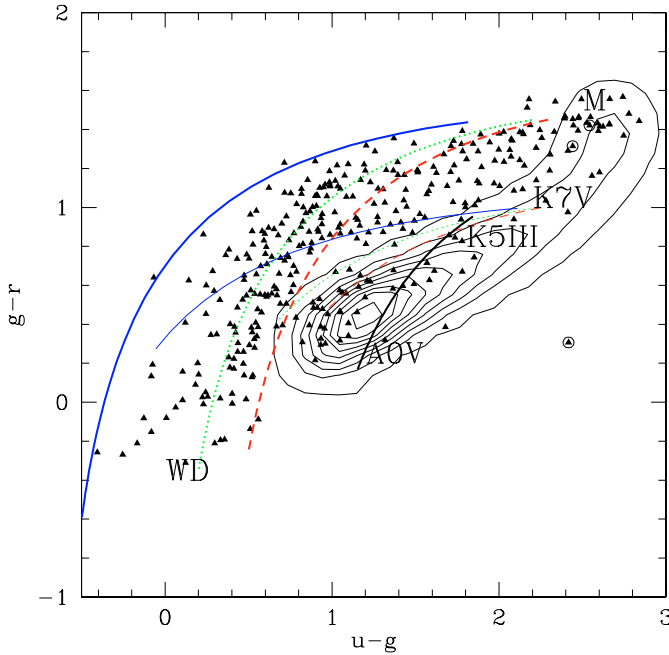


**Fig. 3.** Observed distribution of the angles and separations between the photocenters in  $u$  and  $z$ . The upper-right corner delimited by the dashed lines corresponds to our revised selection criterion.

the displacement and colors of all these 2230 objects are consistent with the asteroids already identified in SDSS (Ivezić et al. 2002; Jurić et al. 2002). In the case of asteroids, the position of the photocenter changes from  $u$  to  $z$  because of the genuine displacement of the object on the sky in between the two exposures. Because of the way the  $u$  and  $z$  CCDs are located on the detector (the scanning order is *riuzg*), the positions in  $u$  and  $z$  are on the same side with respect to the  $r$ -positions, thus yielding a null angle.

In the single star simulation, the distribution of the angle between the  $u$  and  $z$ -photocenters shows a continuous decrease towards  $\pi$ . However the lower panel of Fig. 3 reveals that, once out of the asteroid region of the distribution, the number of large angles actually increases, which is consistent with the presence of binaries.

Even though the distribution shows an increase from  $0.2$  rad up to  $\pi$  and the simulation indicates that no single star is likely to cause a displacement larger than  $0.3''$ , we conservatively adopt  $1.5$  rad and  $0.5''$  for the lower bounds of the angle and separation respectively. This final cut leads to 346 candidate binaries listed in Table 1. There is no noticeable clustering of these objects in chip coordinates nor in  $(\alpha, \delta)$  which rules out the possibility of an instrumental (e.g. corrupted CCD row or column) or observational (e.g. unnoticed bad seeing) problem which would have caused the displacement. According to the simulations, no single star out of 4 millions objects contaminates our sample of binaries.



**Fig. 4.** Color-color diagram of the putative binaries (triangles) superposed over the original parent population of 284 503 stars (contours). The thick/thin lines represent systems with a M dwarf/K7V component. The short thick line close to the center corresponds to A0V+K5III systems. Triangles with a circle around have weird colors that could be the cause of the displacement.

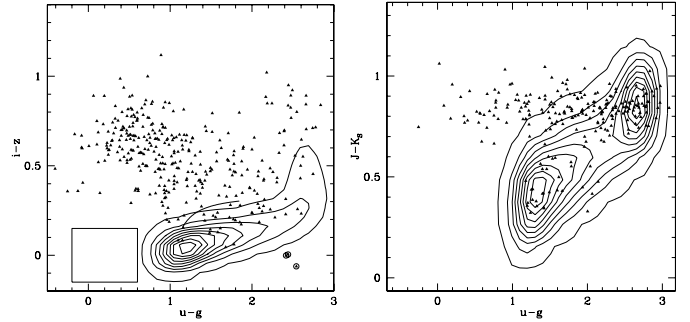
## 5. Results

### 5.1. WD+MD bridge

If the components of a binary have different colors, the resulting colors of the system do not all match single star ones. Whereas most combinations of stellar colors remain consistent with the stellar locus, any departure from the latter can be interpreted as the signature of the duplicity of the source. Smolčić et al. (2004) used that color selection to identify a second stellar locus in the SDSS data, namely a bridge in the  $u-g$  vs.  $g-r$  color-color diagram between white and M dwarfs.

Our 346 candidate binaries are displayed in the same color-color diagram in Fig. 4. Although the two techniques are rather orthogonal, our purely astrometric approach reproduces the essence of the color-based results after Smolčić et al. (2004). Such a result was expected since those two groups of stars have the largest color difference but are of similar absolute magnitudes and are therefore the most likely to yield a noticeable displacement between the  $u$ - and  $z$ -photocenters. Only 53 objects match the criteria of brightness and colors imposed by Smolčić et al., i.e. 6% of their bridge stars match our astrometric criteria.

In order to explain the bottom-left part of the diagram, one cannot rely on the assumption of a unique color for all the white dwarfs, especially in  $u-g$  and  $g-r$ . Following Harris et al. (2003) we instead adopt three different model WDs to cover the range of  $u-g$ , yet keeping  $r-i = i-z = 0$ . The coordinates of the three WDs in the  $(u-g, g-r)$  plane are respectively



**Fig. 5.** *Left panel:* alternative color-color diagram. The rectangle is the locus of quasars after Richards et al. (2001). The curve is the track of A0V+K5III systems. *Right panel:* SDSS-2MASS color-color diagram of 241 SDSS CID binaries matched in the 2MASS database. M stars have  $J-K_s \sim 0.8$ .

$(-0.5, -0.6)$ ,  $(0.2, -0.35)$ ,  $(0.5, -0.25)$ . The WD colors adopted by Smolčić et al. (2004) lies between our second and third models. The flux ratio between the white dwarf and the M dwarf is assumed to range between 0.01 and 100.0. The three resulting tracks are plotted as thick lines in Fig. 4.

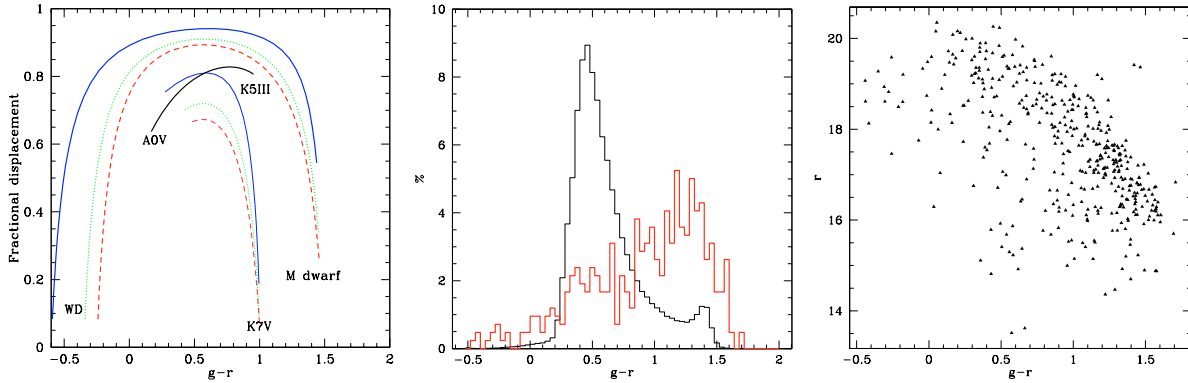
Since at least one of our extended bridges passes over the quasar region of the  $(u-g, g-r)$  diagram, could it be that some of our candidates binaries are actually QSOs? From the  $i-z$  of these points (Fig. 5), one can conclude that it is seldom (if ever) the case (according to Richards et al. (2001), QSOs have  $i-z \sim 0$ ). All the questionable points are hence consistent with a white dwarf + M dwarf pair.

### 5.2. Additional models

Owing to the narrow convergence of the three tracks at the M dwarf end, only 76% of the points are bounded by the previous models. What other combinations of stars would produce system colors consistent with the data? As we have already stated, the colors have to be rather different and yet the magnitudes to be rather similar. Assuming a WD companion, the bluer the main sequence component, the larger the magnitude difference and the more similar the colors.

If the M dwarf is replaced with, say, a K7 main-sequence star (assuming 2.32, 1.01, 0.32, and 0.15 for  $u-g$ ,  $g-r$ ,  $r-i$ , and  $i-z$  respectively based on the list after Gunn & Stryker (1983) convolved with the SDSS filters (Fukugita et al. 1996)), the flux ratio in the  $r$  band becomes a bit more constrained:  $2.5F_{r,K} \leq F_{r,WD} < 250F_{r,K}$ . The different tracks leading to the same three model white dwarfs as in Sect. 5.1 are plotted as thin lines in Fig. 4. Because of the flux ratio constraint, these tracks do not go down to the WD region but that part of the diagram is already covered by the WD+MD model anyway.

Almost 90% of the candidate binaries can thus be explained with a model involving a WD and any main-sequence star redder than K7. What about the remaining 10% whose  $(u-g, g-r)$  cannot that easily be explained with any of the previous scenarios? Even though several of these points are located around  $(1.1, 0.4)$  in the  $(u-g, g-r)$  diagram, i.e. they are consistent with the peak of the stellar locus and hence with a



**Fig. 6.** *Left panel:* ratio of  $\|(u, z)\|$  over the actual angular separation of the two components. The thick (resp. thin) lines represent systems with a M dwarf (resp. K7V) component. The short thick line in the upper right corresponds to A0V+K5III systems. *Central panel:* distribution of the  $g - r$  color of the parent population (thin line) and the binaries (thick line). *Right panel:* color–magnitude of the putative binaries.

possible contamination by weird single stars, that region is totally depleted in the  $(u - g, i - z)$  diagram (Fig. 5).

Besides the binaries with a WD component, what other systems could exhibit large displacements between the  $u$  and  $z$  filters? A A0 main-sequence and a giant K5 have rather similar magnitudes, yet rather different colors (almost as much as the WD+MD pairs). The flux ratio in the  $r$  band between the two components is constrained to the range 0.63–6.3. For the K5 giant (resp. A0V), we adopt the colors 3.40 (1.01), 1.35 (−0.21), 0.56 (−0.14), and 0.33 (−0.11) for  $u - g$ ,  $g - r$ ,  $r - i$ , and  $i - z$  respectively (Gunn & Stryker 1983; Fukugita et al. 1996). The corresponding track is displayed in both Figs. 4 and 5 (left panel) as a thick line. It is worth noting that this track is consistent with the stellar locus in both diagrams thus confirming that the CID binaries would not all be identified as outliers in a color–color diagram.

Even though 2MASS does not go as faint as SDSS, the overlap between the two surveys (Finlator et al. 2000) is nevertheless large enough to obtain combined color–color diagrams for 241 of our putative double stars (~70%). Among the combinations of filters, the  $u - g$  vs.  $J - K_S$  exhibits the largest departure of these binaries from the stellar locus (right panel of Fig. 5). Instead of a bridge as in Fig. 4, the binary locus appears as a narrow horizontal band in the combined 2MASS SDSS diagram. Unlike the SDSS colors, the 2MASS color allows us to rule out the possibility for the M stars to be giant rather than dwarf. Note also that there are still CID binaries whose colors are very consistent with the main stellar locus even when 2MASS bands are used as well.

### 5.3. Contamination

Three stars have weird colors (triangles with a circle around in Figs. 4 and 5), especially in  $i - z$ , which is below −0.5 for six of them. In such cases, the noticed displacement would be caused either by the wrong astrometric transformation or by the wrong correction of the atmospheric refraction both resulting from the unusual colors rather than by a true displacement of the photocenter. However spectra available for some of these troublesome points confirm the duplicity. So, in the worst case, the contamination rate does not exceed 1%.

### 5.4. Angular separation

The likelihood of detecting a CID binary clearly depends on the difference in colors of the components but it also depends on the actual angular separation of the two stars. From the only criterion adopted so far, namely  $\|(u, z)\| > 0.5''$ , what can we infer about that angular separation? The ratio of  $\|(u, z)\|$  to that separation is plotted in the left panel of Fig. 6.

All the white dwarf systems show a maximum displacement above  $g - r = 0.5$ , corresponding to 60%, so any separation larger than  $0.85''$  fulfills the criterion. That is consistent with the distribution plotted in the central panel of Fig. 6. It shows that whereas the parent distribution peaks below  $g - r = 0.5$ , the binary distribution peaks well above that value.

Whereas the fractional displacement starts decreasing above  $g - r = 0.7$ , the binary distribution keeps growing up to  $g - r \sim 1.3$  where the displacement has already decreased to 70%. This means that the decrease of the fractional displacement is compensated by the actual angular separation of the components. Assuming a constant linear separation, these systems should thus be closer. A color-magnitude diagram (right panel of Fig. 6) gives credit to that explanation. Indeed, the redder, the brighter while the absolute magnitude goes up thus meaning that the reddest objects are on average closer to us.

## 6. Conclusions

The color induced displacement method (Christy et al. 1983; Sorokin & Tokovinin 1985; Wielen 1996; Bailey 1998) as a way of detecting binaries has been successfully applied to the second public release of the SDSS data. We identify about 350 systems whose changes in position are essentially consistent with a white dwarf coupled to a lower end (later than ~K7) main-sequence star. We therefore expect ~1000 CID binaries at the completion of the SDSS observation campaign.

This identification of binaries is an independent confirmation of the color based results of Smolčić et al. (2004). However, whereas they had a lower bound on  $g - r$  of 0.3, the astrometric criterion allows us to identify candidate binaries down to  $g - r = -0.4$ . On the other hand, color selection they utilized is more sensitive to binaries with angular separations smaller than the sensitivity of the CID method.

Though the approach has proven to give results, its efficiency is extremely low. Whereas Marchal et al. (2003) quote at least 30% of binaries among M stars (the percentage grows with the mass of the star along the main-sequence), only 0.02% are detected through their CID effect. It is noteworthy that with such a low fraction, the CID binaries do not affect the overall SDSS astrometric precision.

Because of their much better astrometric precision (typically a few  $\mu\text{s}$ ), space-based astrometry missions like SIM and Gaia will eventually supersede the SDSS results presented here. According to a Gaia preparatory study (Arenou & Jordi 2001), the latter could, for instance, detect a M0 companion to a G0 dwarf star at a  $3\sigma$  level at a separation as low as 2.3 mas. In terms of separations, this is  $\sim 200$  times better than the sensitivity of the CID method applied to the SDSS data. However, the precision of the Gaia astrometry will be worse than 2.3 mas at the fainter magnitudes typical of the objects studied in the present paper, so the expected improvement in the number of CIDs detected cannot be reliably estimated.

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## Appendix A: SQL code

Besides the criteria related to the photometric precision and the astrometric displacement, the way the image was processed is also taken into account. The resulting code, once submitted to DR2, returns both the CID and the asteroids. The final step of the selection, based on the angle between the photocenters, is left out of the SQL code. Indeed, although the output table would be smaller, the time taken by the query would be much longer since it would imply some computations a database manager system cannot carry on efficiently.

```
declare @BRIGHT bigint set @BRIGHT=dbo.fPhotoFlags('BRIGHT')
declare @EDGE bigint set @EDGE=dbo.fPhotoFlags('EDGE')
declare @SATURATED bigint set @SATURATED=dbo.fPhotoFlags('SATURATED')
declare @NODEBLEND bigint set @NODEBLEND=dbo.fPhotoFlags('NODEBLEND')
declare @bad_flags bigint set @bad_flags=(@SATURATED|@BRIGHT|@EDGE|\
@NODEBLEND)
```

```
select run,rerun,camcol,field,obj,colc,rowc,parentID,nChild,ra,dec,
extinction_r,psfMag_u,psfMag_g,psfMag_r,psfMag_i,psfMag_z,
psfMagErr_u,psfMagErr_g,psfMagErr_r,psfMagErr_i,psfMagErr_z,
rowc,colv,rowvErr,colvErr,rowc_u,colc_u,rowc_g,colc_g,rowc_r,
colc_r,rowc_i,colc_i,rowc_z,colc_z,offsetRa_u,offsetDec_u,
offsetRa_g,offsetDec_g,offsetRa_r,offsetDec_r,offsetRa_i,
offsetDec_i,offsetRa_z,offsetDec_z
into MyDB.CID
from Star
where (flags & @bad_flags) = 0 and nChild=0
and abs(psfMag_u)<21 and abs(psfMag_g)<21
and abs(psfMagErr_u)<=0.1 and abs(psfMagErr_r)<=0.1
and abs(psfMagErr_g)<=0.05 and abs(psfMagErr_i)<=0.05
and abs(psfMagErr_z)<=0.05
and sqrt((offsetRa_u-offsetRa_z)*(offsetRa_u-offsetRa_z)
*cos(dec*0.01745)*cos(dec*0.01745)\
+(offsetDec_u-offsetDec_z)*(offsetDec_u-offsetDec_z))>=0.2
```

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